

NEELS Data ex

Empirical Exs. Multilevel 10 schools ex.

Kreft + De Leeuw
text Week 4
Stat 209

①

Math ach
(Y)
on
homework
(X)

INTRODUCING MULTILEVEL MODELING

Table 2.4 Aggregate regression for 10 schools $Y_{on} \bar{X}$

	Null model		With homework	
	EST	SE	EST	SE
Intercept	51.3	2.44	37.1	4.03
Slope b_B	n.a.		7.0	1.84
R^2	0.00		0.64	
$\hat{\sigma}$	39.3		24.9	

$$\beta_{yx}^T = 3.6$$

NEELS data in
influence.ME
package

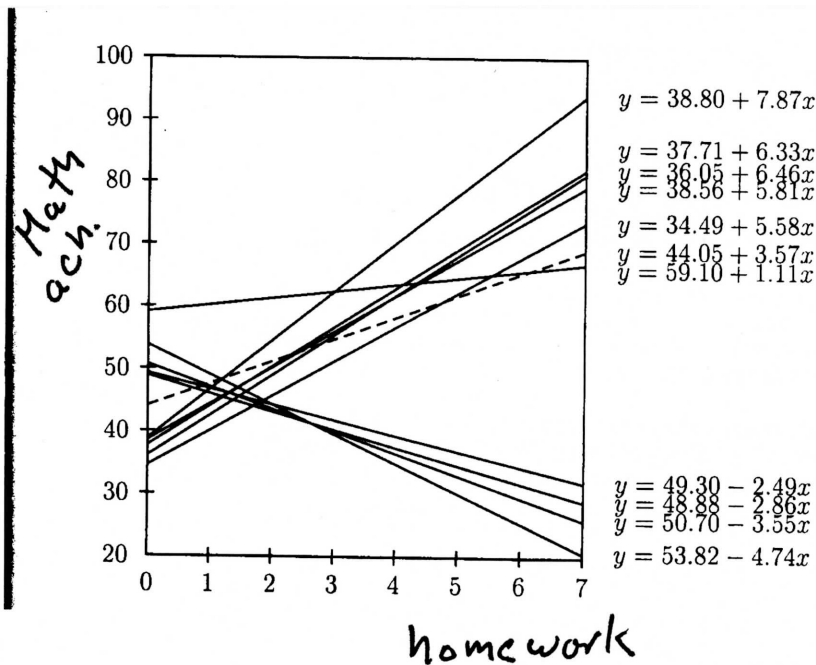
Table 2.6 Cronbach model for 10 schools $Y_{on} x - \bar{x}, \bar{x} - \bar{x}$

	Null model		With homework	
	EST	SE	EST	SE
Intercept	51.3	0.69	37.1	1.46
Slope b_W		n.a.	2.1	0.43
Contextual effect b_B		n.a.	7.0	0.67
R^2		0.00		0.34
$\hat{\sigma}$		11.1		9.0

Table 2.5 Contextual model for 10 schools $Y_{on} X, \bar{X}$

	Null model		With homework	
	EST	SE	EST	SE
Intercept	51.3	0.69	37.1	1.46
Slope b_W		n.a.	2.1	0.43
Contextual effect $b_B - b_W$		n.a.	4.9	0.79
R^2		0.00		0.34
$\hat{\sigma}$		11.1		9.0

w/in school fits (n=10)



"slopes as
outcomes"
(multilevel
analysis)

why slopes
differ?
school type etc.

Y on X, \bar{X}
Y on X, $X - \bar{X}$
Y on $X - \bar{X}$, \bar{X}

$$b_{YX\bar{X}} = b_w, \quad b_{Y\bar{X}X} = b_B - b_w$$

$$b_{YX(X-\bar{X})} = b_B, \quad b_{Y(X-\bar{X})X} = b_w - b_B$$

$$b_{Y(X-\bar{X})\bar{X}} = b_w, \quad b_{Y\bar{X}(X-\bar{X})} = b_B \quad \text{orthogonal}$$
(15)

as if by experiment?

Substantive Interpretations and Estimators of Individual, Contextual, and Frog Pond Effects of Ability on Achievement in Classrooms in Two-effect Models

Type of Effect	Alternative Interpretations	Estimators from Equations 11-13
Individual	A student's ability affects the student's learning and hence measured achievement	$b_{YX(X-\bar{X})}$ β^b
Contextual	Psychological (opportunity to learn)—group ability affects instructional practice (e.g., amount of instructional time, topics covered) which, in turn, affects individual learning and achievement	$\beta^b - \beta^w$
Frog Pond	Psychological (opportunity to learn)—the student's <u>relative standing</u> within the group affects the allocation of instructional resources and style of instruction provided the student and thereby the student's learning and achievement	$b_{Y(X-\bar{X})\bar{X}}$ $b_{Y(X-\bar{X})X}$
	Sociological (relative status effects)—relative standing in the group affects individual motivation to learn and thereby individual learning and achievement	

effect of group membership on individual behavior

see within groups effects

For a single independent variable, the equation for the contextual effects model can be written as

$$Y_{ij} = a_Y + b_{YX\bar{X}}X_{ij} + b_{Y\bar{X}X}(\bar{X}_i - X_{ij}) + u_{ij}, \quad (11)$$

where Y_{ij} and X_{ij} are individual-level measures on Y and X for person j in group i, \bar{X}_i is the mean for group i on variable X, and u_{ij} is a random disturbance term with the usual least squares properties. This equation is the same as Firebaugh's (1978) equation for detecting cross-level bias (Equation 9)

performance. A model that specifies that individuals' absolute (X_{ij}) and relative ($X_{ij} - \bar{X}_i$) standing on some characteristic both affect their outcomes can be written as

$$Y_{ij} = a_Y + b_{YX(X-\bar{X})}X_{ij} + b_{Y(X-\bar{X})\bar{X}}(X_{ij} - \bar{X}_i) + u_{ij}, \quad (12)$$

with $b_{YX(X-\bar{X})}$ measuring the individual effect and $b_{Y(X-\bar{X})\bar{X}}$ measuring the frog pond effect. If, instead, it is believed that individual outcomes are affected by the group level (\bar{X}_i) and the individual's relative standing in the group ($X_{ij} - \bar{X}_i$), the model can be written as

$$Y_{ij} = a_Y + b_{Y(X-\bar{X})\bar{X}}(X_{ij} - \bar{X}_i) + b_{Y\bar{X}(X-\bar{X})}\bar{X}_i + u_{ij}, \quad (13)$$

where $b_{Y(X-\bar{X})\bar{X}}$ and $b_{Y\bar{X}(X-\bar{X})}$ are interpreted as measures of frog pond and contextual effects, respectively.

$X_i, X - \bar{X}$

$X - \bar{X}, \bar{X}$