

## Exam Data: Mixed effects models (gender gap)

prelim SFYS (ImList)

$$\text{normexam } Y = \alpha_0 + \alpha_1 \text{sexM} + \epsilon \quad \text{by school}$$

$$\hat{\alpha}_0 = \bar{Y} \quad \hat{\alpha}_1 = \bar{Y} - \bar{F}$$

Unconditional Model ggamlmer

$$\text{Level 1 } Y = \alpha_0 + \alpha_1 \text{sexM} + \epsilon$$

$$\text{Level 2 } \alpha_0 = \gamma_{00} + \eta_0 \quad \alpha_1 = \gamma_{10} + \eta_1$$

(fixed)  
(random)

combined model  $Y \sim \text{sex}$  (fixed eff) (sex|school)

Conditional model ggamlmer2 (corrected schavg)

$$\text{Level 1 } Y = \alpha_0 + \alpha_1 \text{sexM} + \epsilon \quad (\text{random})$$

$$\text{Level 2 } \alpha_0 = \gamma_{00} + \gamma_{01} \text{schavg} + \eta_0$$

$$\alpha_1 = \gamma_{10} + \gamma_{11} \text{schavg} + \eta_1$$

(fixed)

combined model  $Y \sim \text{sex} * \text{schavg}$  (fixed eff)

Within-school ANCOVA

ancova|mer

covariate  
standLRT

level 1

$$Y = \alpha_0 + \alpha_1 \text{sexM} + \alpha_2 \text{standLRT} + \epsilon$$

schavg = standLRT

anova

$$\text{Level 2 } \alpha_0 = \gamma_{00} + \eta_0 \quad \alpha_1 = \gamma_{10} + \eta_1 \quad \alpha_2 = \gamma_{20} + \eta_2$$

(could have additional predictors)

combined  $Y \sim \text{sexM} + \text{standLRT}$  (fixed)

effects random fixed

random - varies over schools (Level 1 units)

fixed - does not vary over schools

see plots