

Binary Treatments vs Dose-Response

Binary Treatment T (0/1, T/C)
prima facie $Y \sim T$ $\bar{Y}_T - \bar{Y}_C$

propensity score $T \sim X$, $\hat{E}(T|X)$, $\hat{e}(X)$
eg logistic regression

outcome analysis. One use of $\hat{e}(X)$ (cc. 2) is "matching" by regression interpolation

$Y \sim T + \hat{e}(X)$ simple OLS, coef(T)
or use smoothers to compare $Y \sim \hat{e}(X)$ each group
PSA graphics f ANCOVA packages

Dose-Response, Dose D , ADRF

prima facie $Y \sim D$ or $Y = f(D)$
ignores self-selection into Dose level

Hirano-Imbens

GPS Generalized Propensity Score

GPS = $\hat{E}(D|X)$ predict Dose from confounders level

outcome analysis

use GPS and chosen Dose to predict Y

$Y \approx f(\text{GPS}, D)$ e.g. 2nd degree polynomial

plot fit vs D estimate ADRF